



# Meso-macro simulation of the draping of composite textile reinforcements

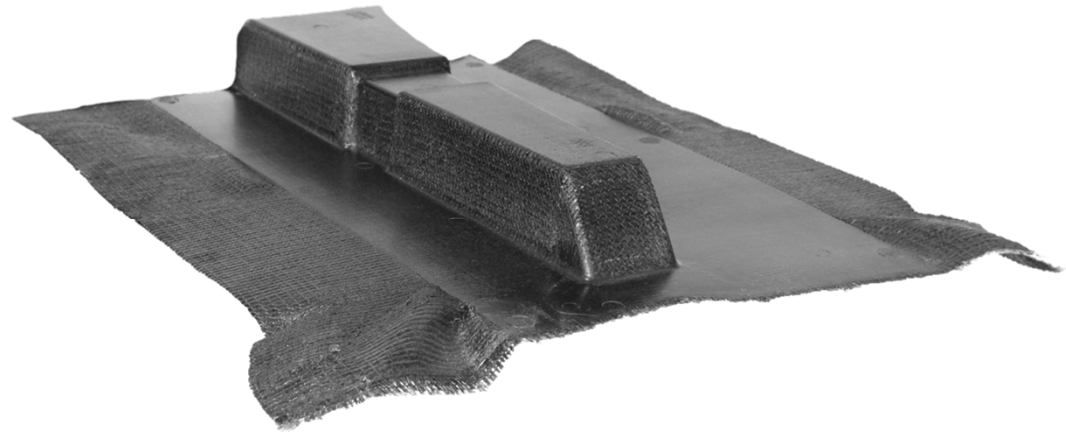
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1 : Engineering Development Center,  
Toray Industries, Inc., 3-1 Sonoyama 3-chome , Ostu, Shiga 520-0842 Japan

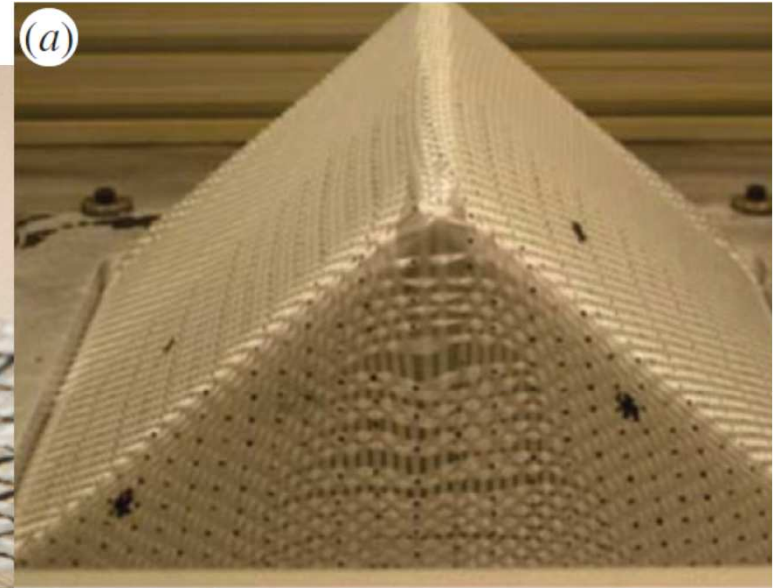
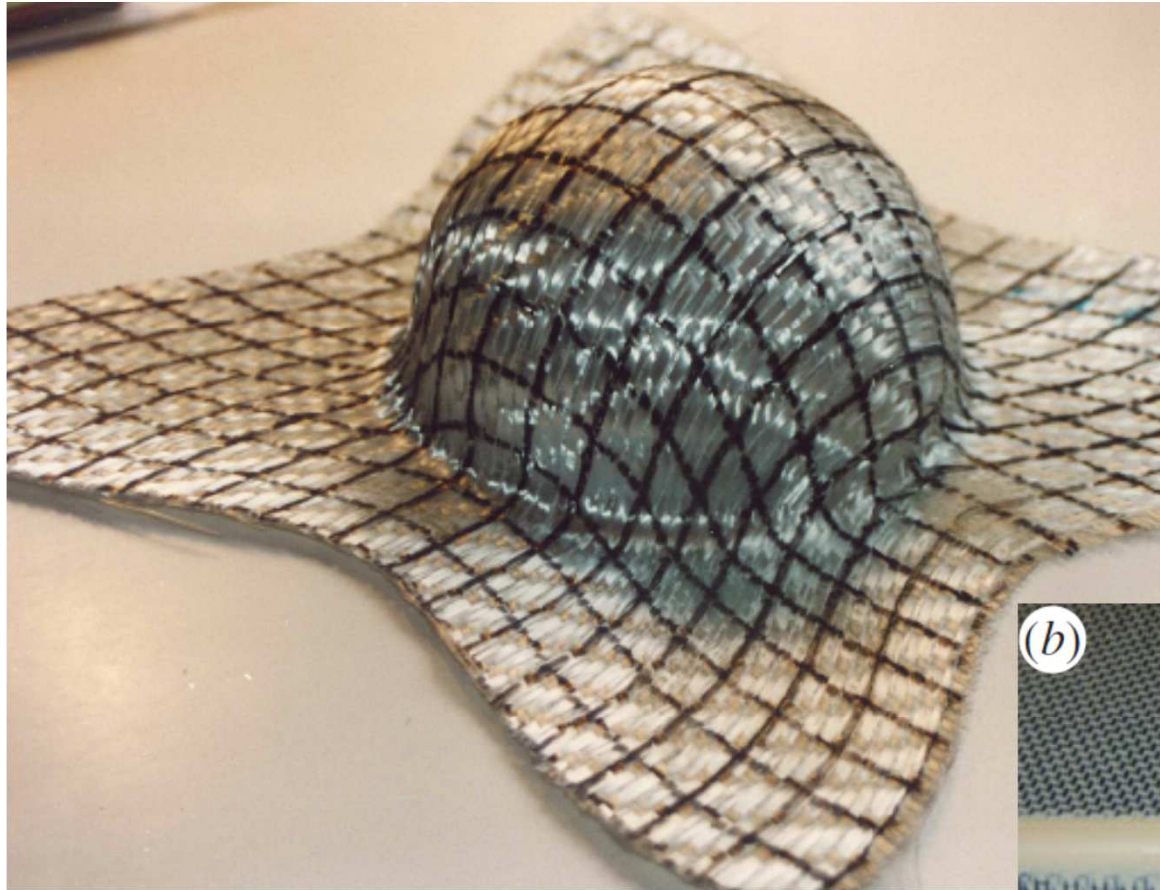
2 : LaMCoS, Université de Lyon, CNRS, INSA Lyon, France

3 : Department of Materials Engineering,  
KU Leuven, Kasteelpark Arenberg 44, BE-3001 Leuven, Belgium

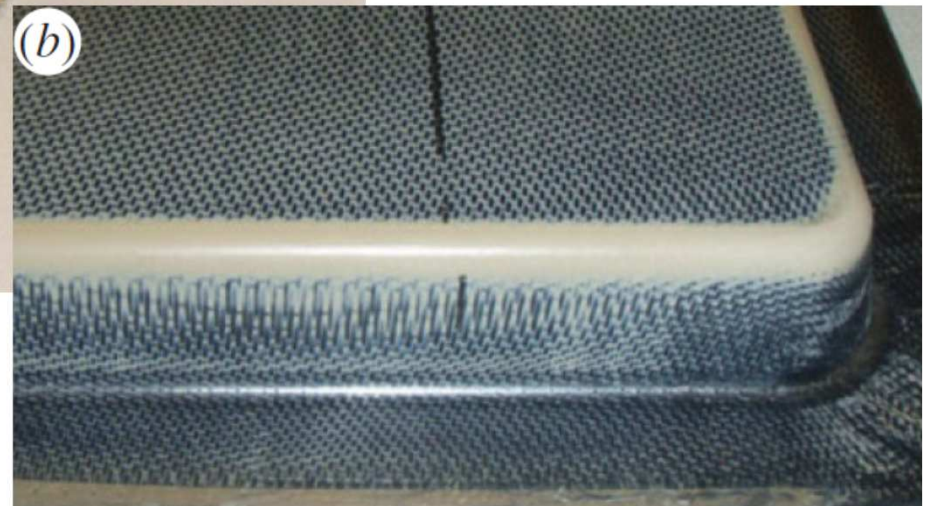
# Textile composite parts with double curved geometry



Composite reinforcements made of continuous fibres can be considered as a continuous medium



[Allaoui et al, I. J. Mat. Form. 2014]



[Boisse et al, Phil. Trans. 2016]

This is not always the case.  
Slippages, gaping can occur (defects)

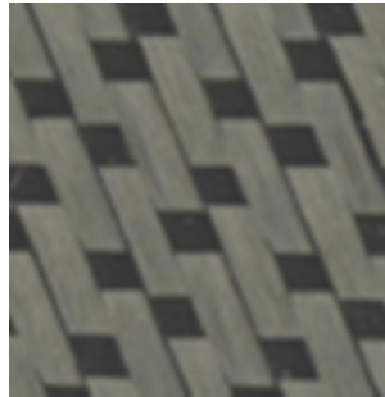


macro



Macroscopic scale  
(scale of the part)

meso



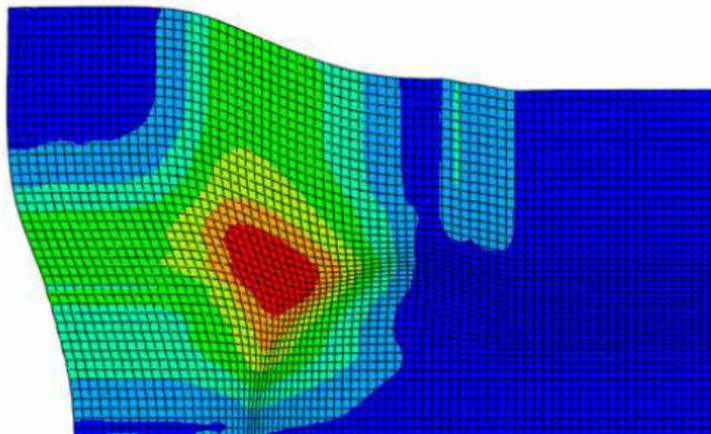
Mesoscopic scale  
(scale of the yarn  
and of the woven cell)

micro



Microscopic scale  
(scale of the fibre)

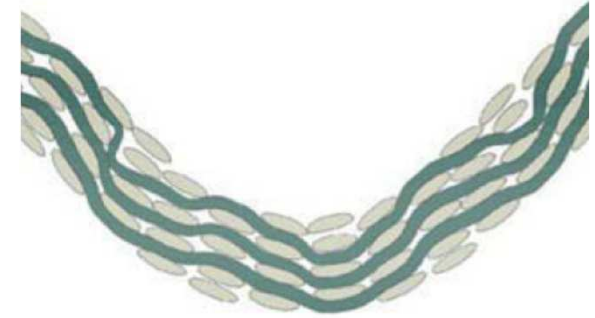
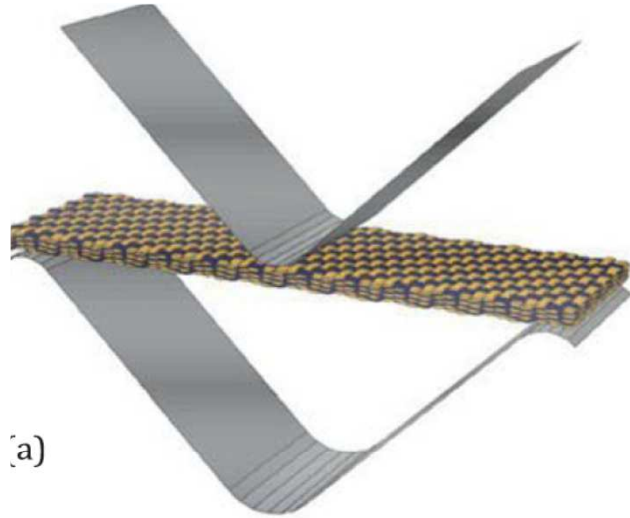
### Three scales for textile reinforcement analyses



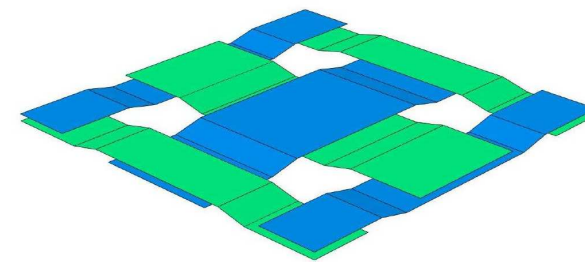
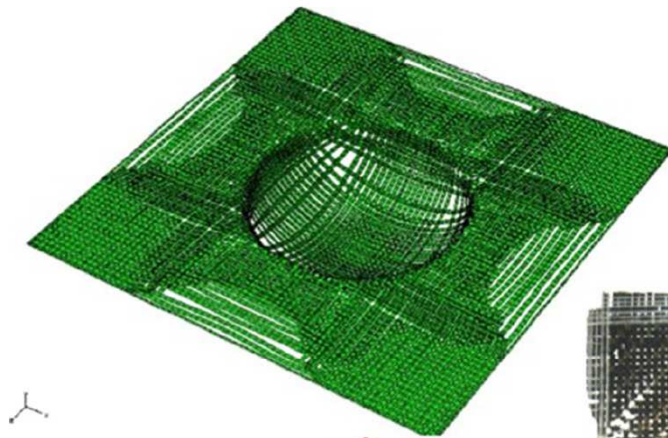
Most of the simulations  
are performed at macro scale

Gaping and local buckling cannot be  
simulated

# Meso FE analyses for the entire preform

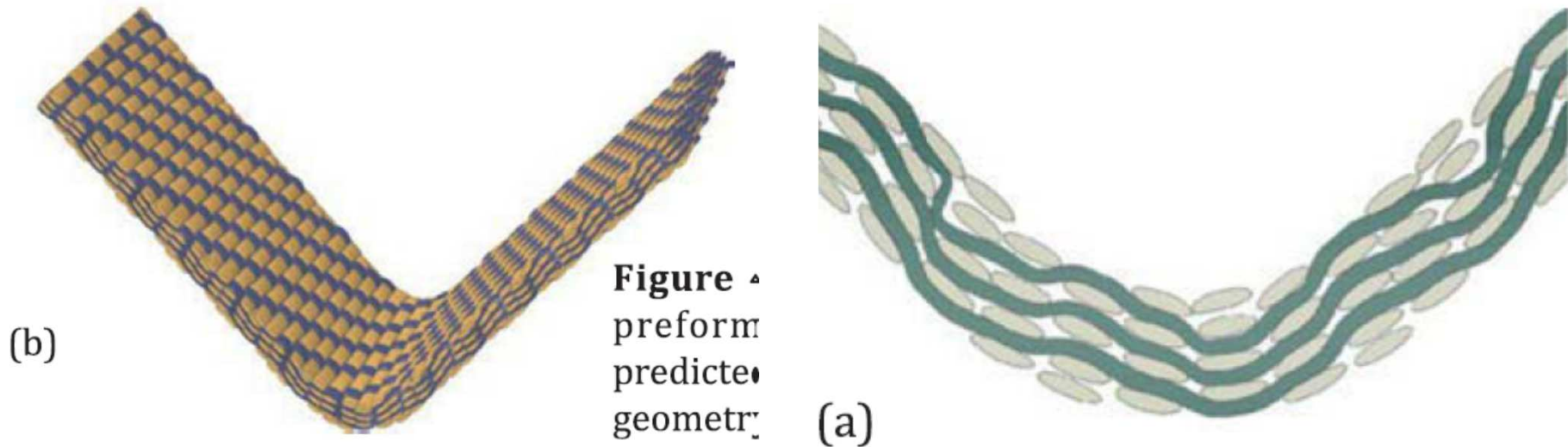


[Bayraktar et al, Sampe J. 2015]



[Gatouillat et al, Composites A 2013]

## Meso FE analyses for the entire preform

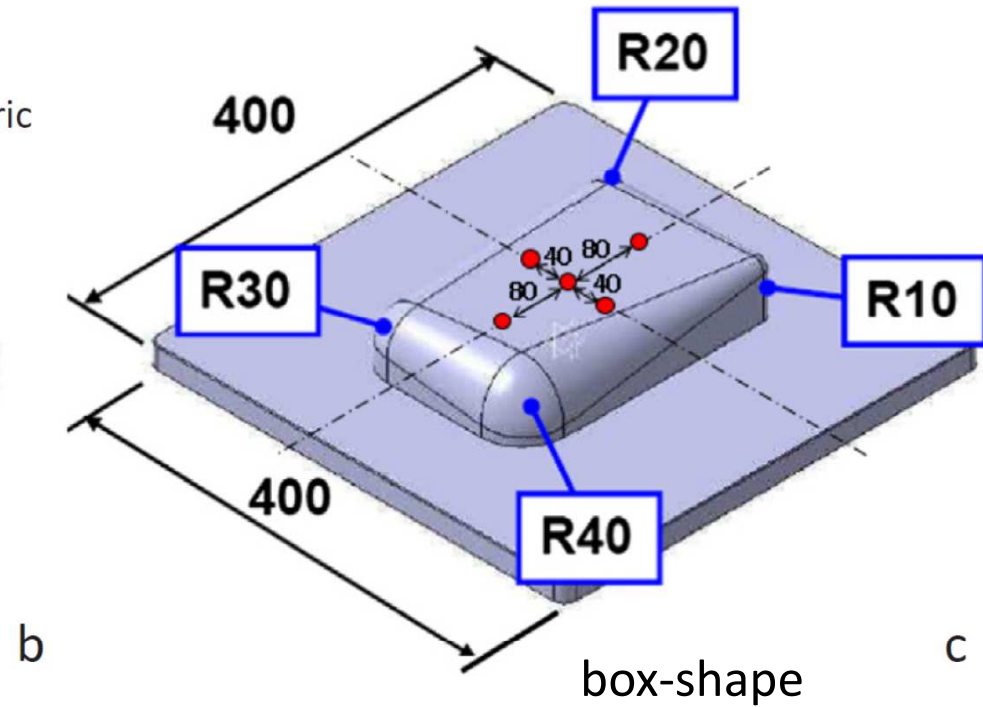
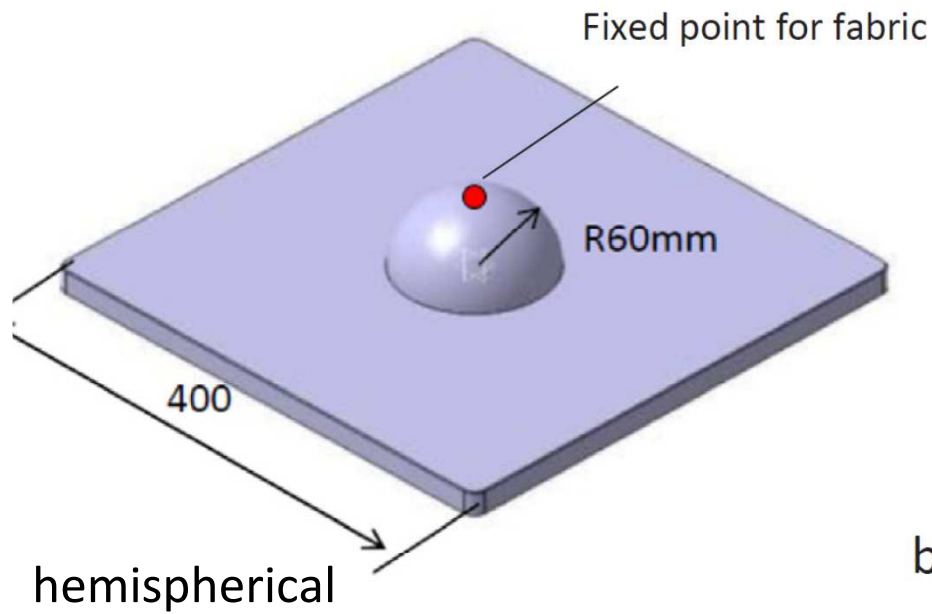


The analyses are complex and require long calculation times

Proposed in this work: A meso-macro approach used to limit the meso calculation to a given area.



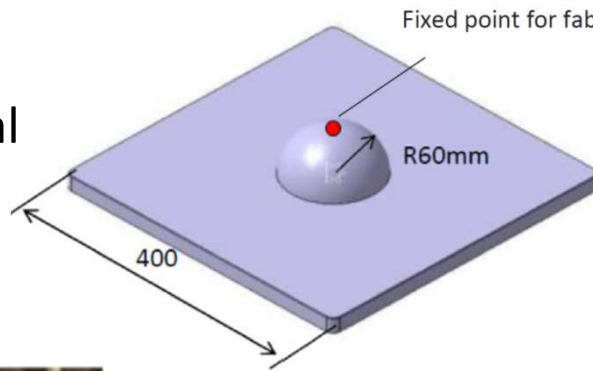
# The geometry considered (double curvature)



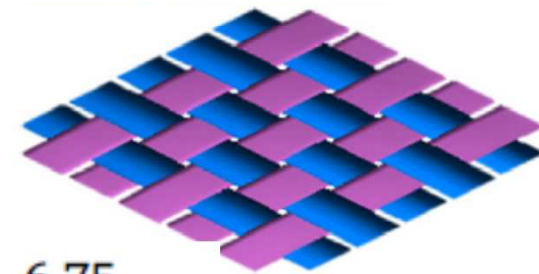
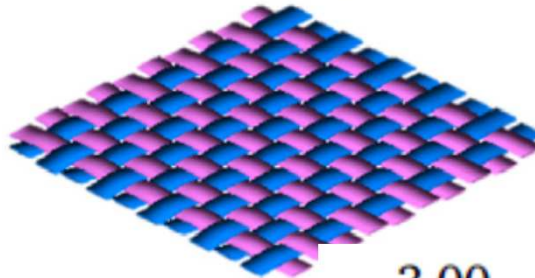
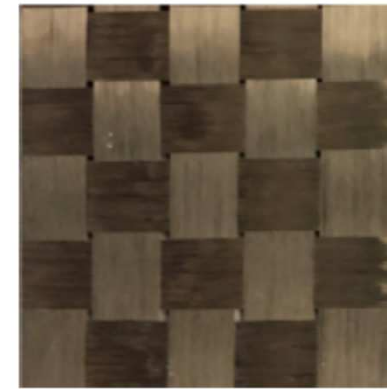
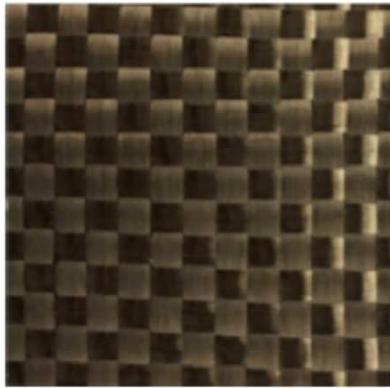
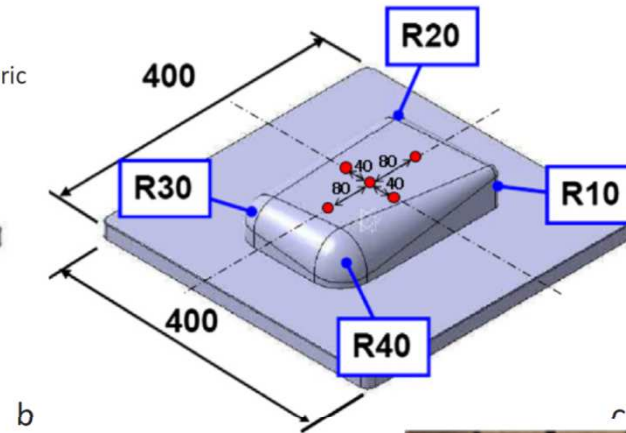
[Iwata et al, Composites A, 2019]

# The reinforcement considered (double curvature)

hemispherical



box-shape



[Iwata et al, Composites A, 2019]

3.00  
0.323  
0.6%

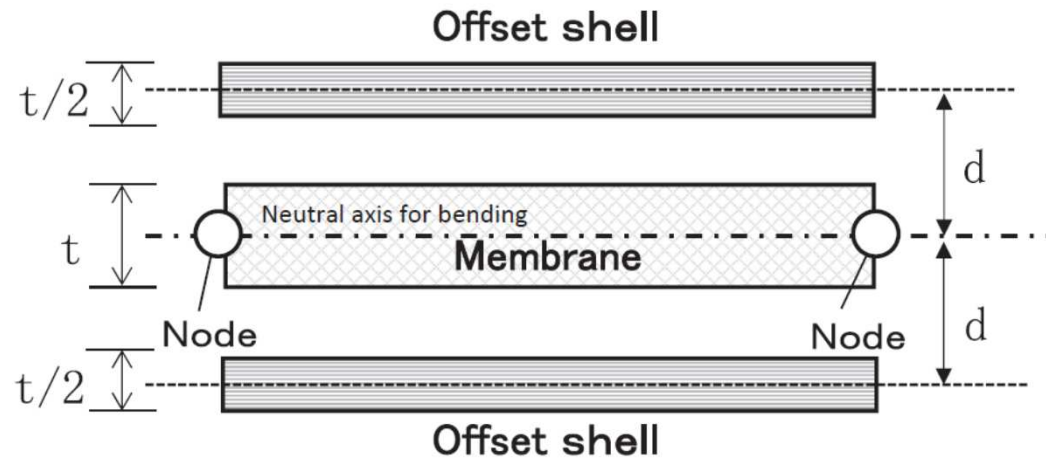
Yarn width, mm  
Yarn thickness, mm  
Crimp, %

6.75  
0.126  
< 0.1%

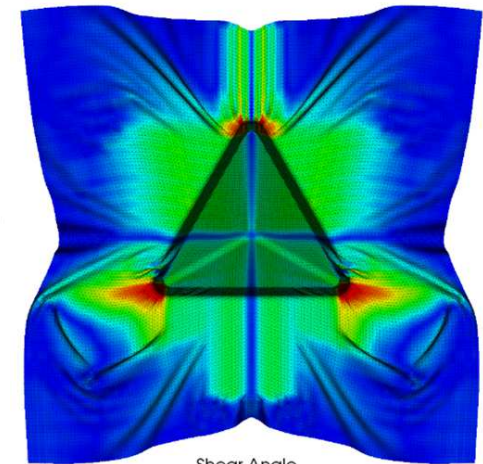


## Constitutive model for the fabric (macro scale)

Macro-draping model, proposed by Nishii et al. [ECCM-16, 2014],



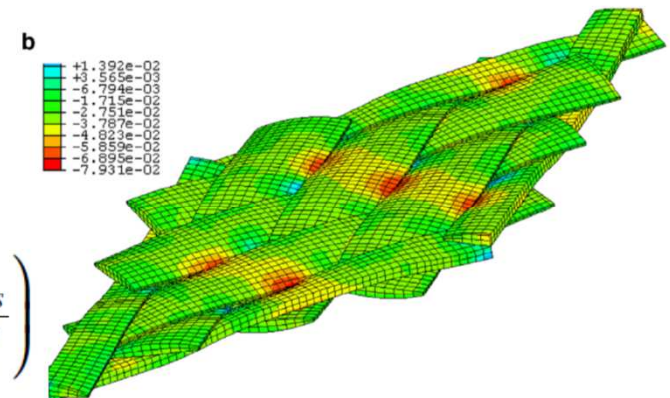
※Two offset shell and membrane share same nodes



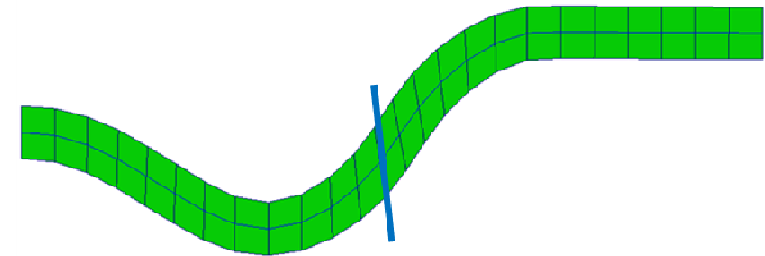
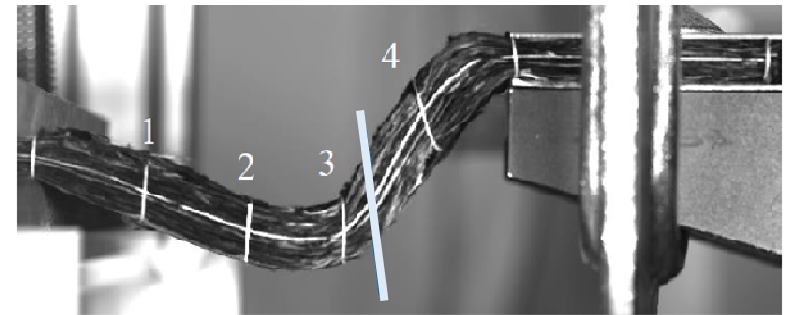
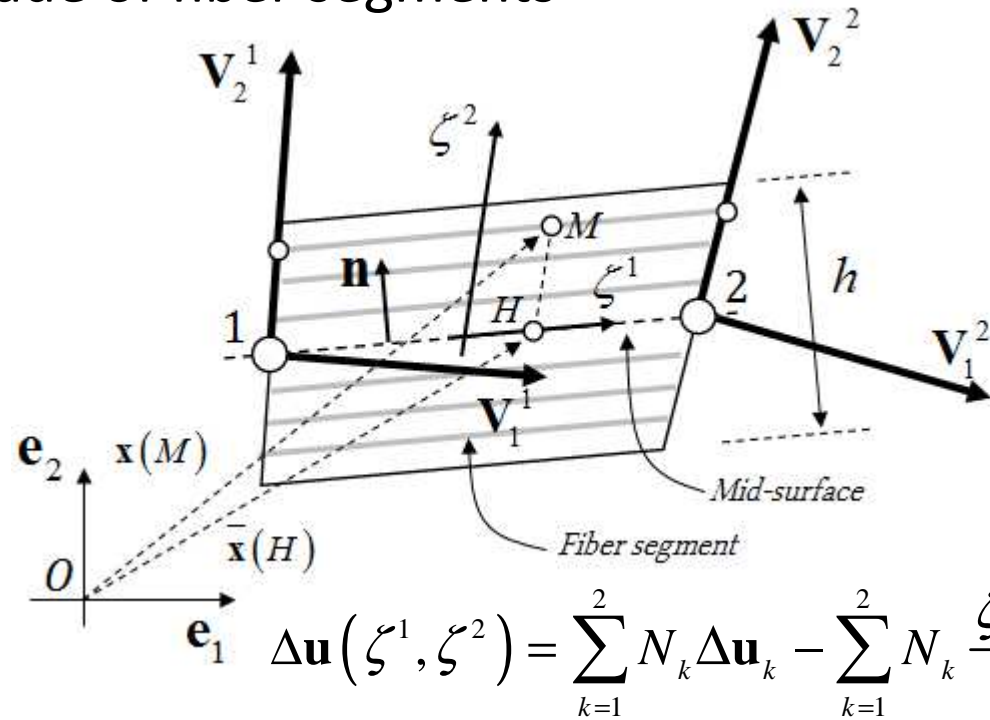
## Constitutive model for the yarn (meso scale)

$$\underline{\underline{S}} = 2 \frac{\partial w}{\partial \underline{\underline{C}}}$$

$$\underline{\underline{S}}_{total} = 2 \left( \frac{\partial w_{elong}}{\partial I_{elong}} \frac{\partial I_{elong}}{\partial \underline{\underline{C}}} + \frac{\partial w_{comp}}{\partial I_{comp}} \frac{\partial I_{comp}}{\partial \underline{\underline{C}}} + \frac{\partial w_{dist}}{\partial I_{dist}} \frac{\partial I_{dist}}{\partial \underline{\underline{C}}} + \frac{\partial w_{cis}}{\partial I_{cis}} \frac{\partial I_{cis}}{\partial \underline{\underline{C}}} \right)$$



# Ahmad Shell element made of fiber segments



Internal virtual work in the element made from fibers

$$\delta W_{\text{int}}^e = \sum_{f=1}^n \int_{L^f} T^{11f} \delta \epsilon_{11}^f dL + \sum_{f=1}^n \int_{L^f} M^{33f} \delta \chi_{33}^f dL$$

[Liang et al, Composites A, 2017]

Tension of fibers

Bending of fibers

The tensile stiffness is large:  
No shear strain energy:

**quasi-inextensibility**  
**possible slippage**

$$W = W(I_1, I_2, I_3, II_4, II_5) \quad \underline{\underline{M}} = \underline{\underline{M}} \otimes \underline{\underline{M}}.$$

$$I_1 = \text{trace}(\underline{\underline{C}}), \quad I_2 = \frac{1}{2}(\text{trace}(\underline{\underline{C}})^2 - \text{trace}(\underline{\underline{C}}^2)), \quad I_3 = \det(\underline{\underline{C}})$$

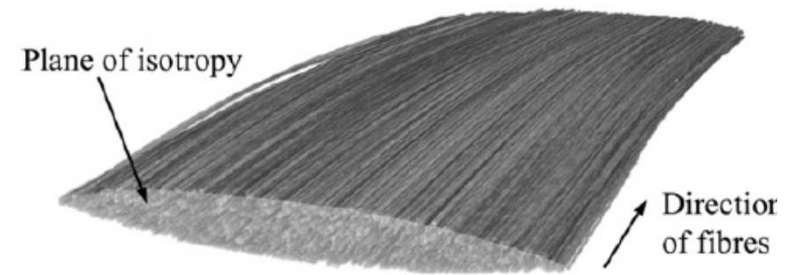
$$II_4 = \underline{\underline{C}} : \underline{\underline{M}} \quad \text{and} \quad II_5 = \underline{\underline{C}}^2 : \underline{\underline{M}}$$

Élongation des fibres :

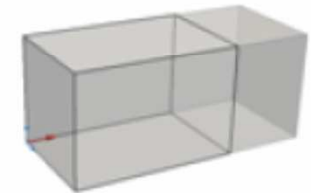
- Grandeur caractéristique : variation de longueur des fibres

- Invariant associé :  $I_{\text{elong}} = I_4 = \underline{\underline{C}} : \underline{\underline{G}}_1$  Énergie associée :

$$W_f(I_4) = \frac{1}{8} \cdot \frac{K}{S_0} \cdot (I_4 - 1)^2$$



Transverse isotropy

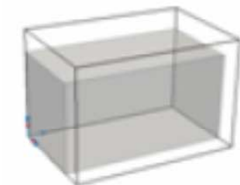


Changement d'aire dans le plan transverse :

- Grandeur caractéristique : variation d'aire de la section transverse (⊥ à la direction des fibres)

- Invariant associé :  $I_{\text{aire}} = \sqrt{\frac{I_3}{I_4}}$  Énergie associée :

$$W_{\text{aire}}(I_4) = k_1 \cdot (I_{\text{aire}}^{-k_2} - 1)^2$$



Changement de forme dans le plan transverse :

- Invariant associé :  $I_{\text{forme}} = \sqrt{I_1 - \frac{I_5}{I_4} - 2I_{\text{aire}}}$  Énergie associée :

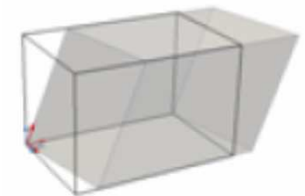
$$W_{\text{trans}}^{\text{forme}}(I_{\text{forme}}) = \frac{1}{2} K_{\text{forme}} I_{\text{forme}}^2$$



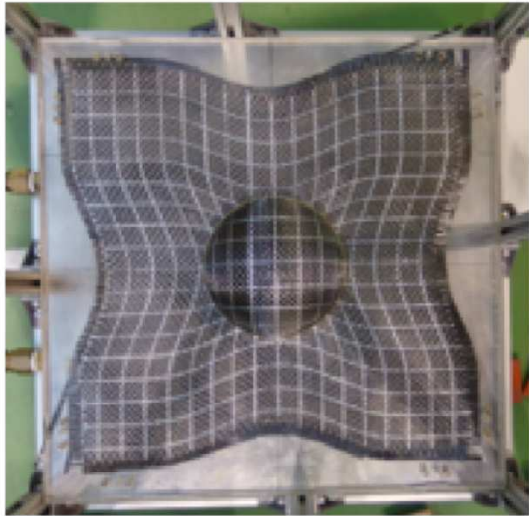
Cisaillement le long des fibres :

- Invariant associé :  $I_{\text{cislong}} = \sqrt{\frac{I_5}{I_4} - I_4}$  Énergie associée :

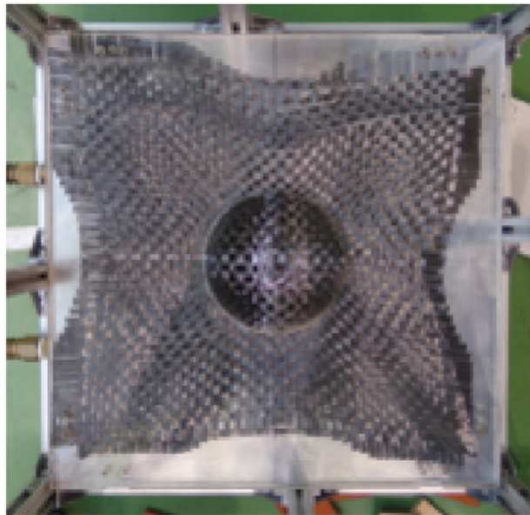
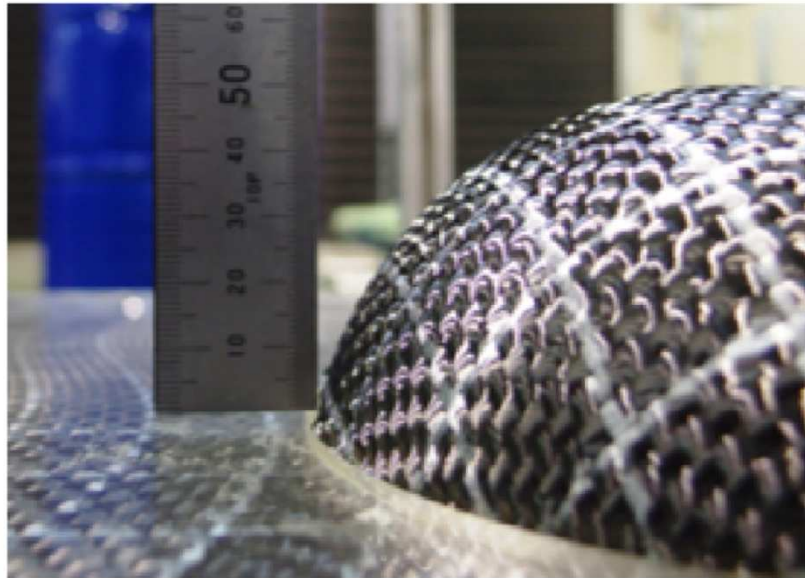
$$W_{\text{cislong}} = \frac{1}{2} K_{\text{cislong}} (I_{\text{cislong}})^2$$





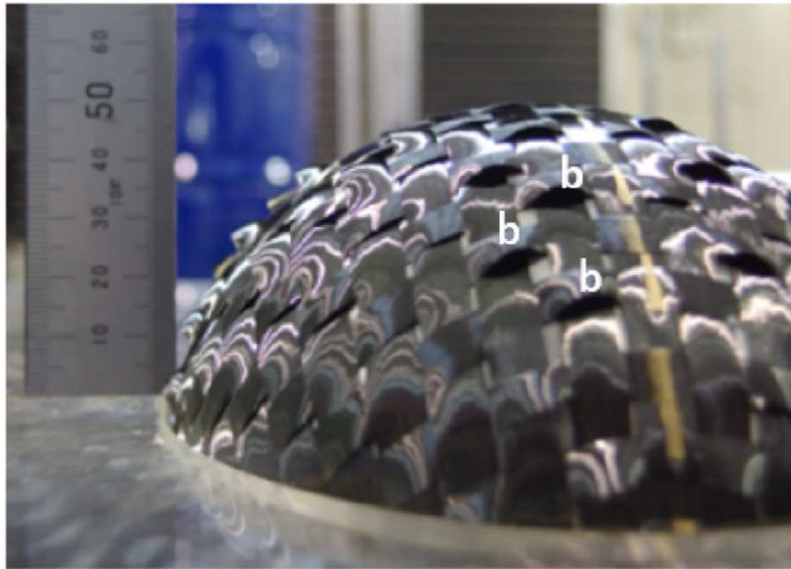


Fabric A



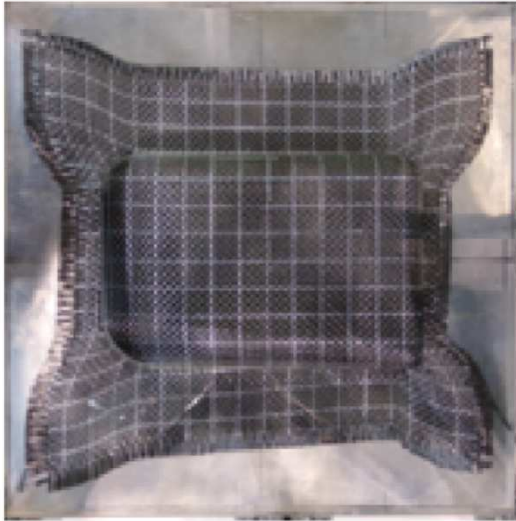
Fabric B

a

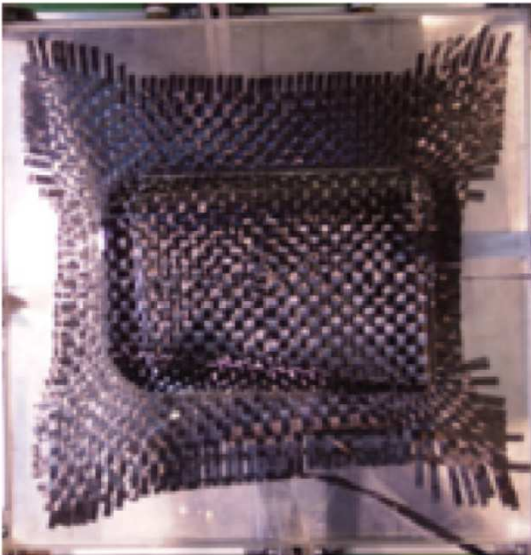
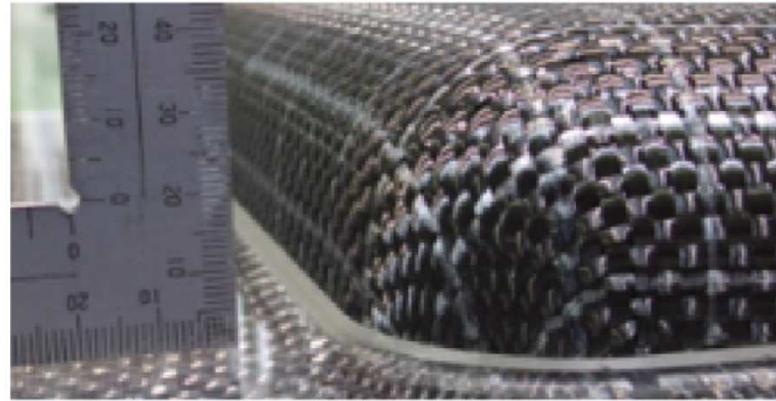


b – buckling

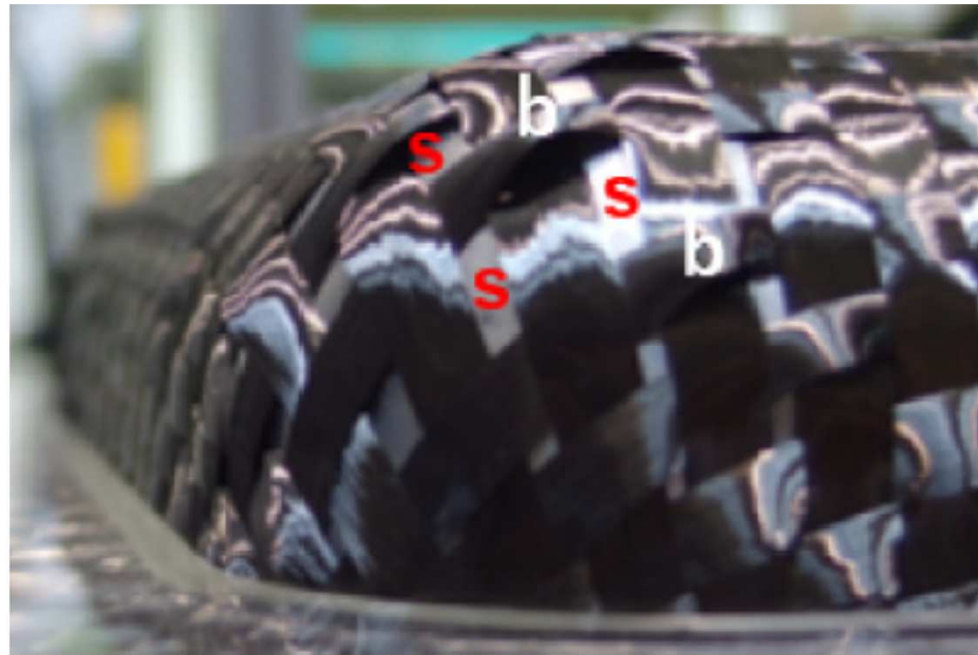
## Hemispherical forming



Fabric A



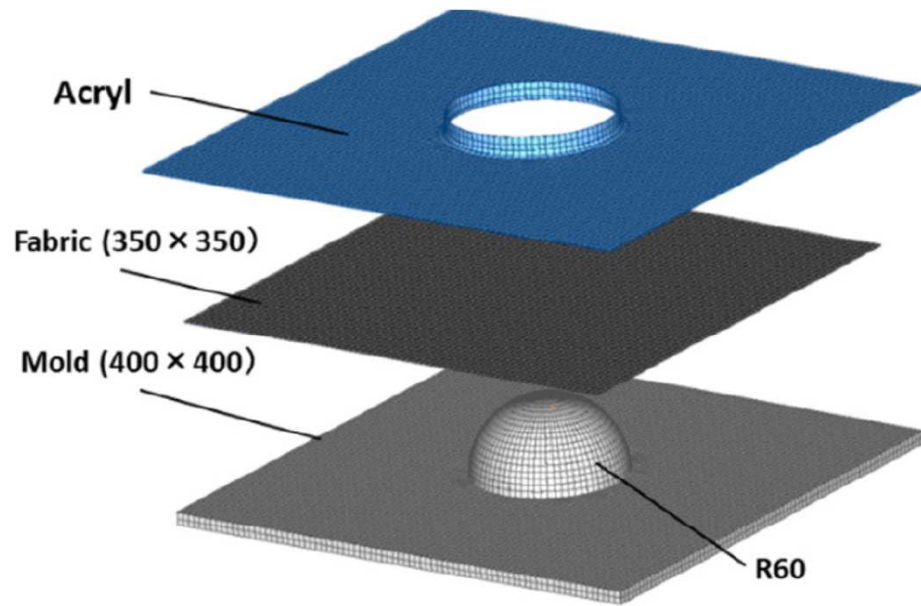
Fabric B



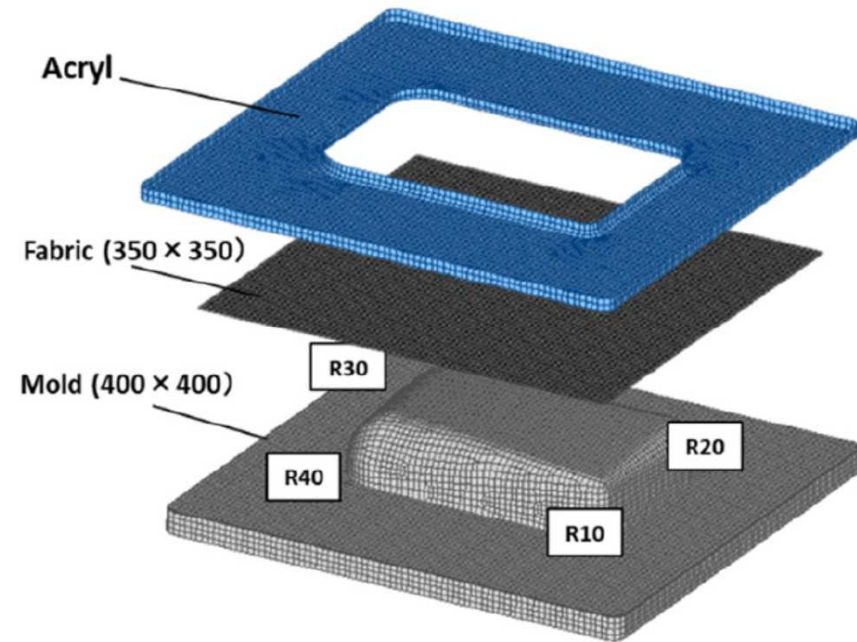
h

box-shaped mould

b – buckling S-sliding



**a**

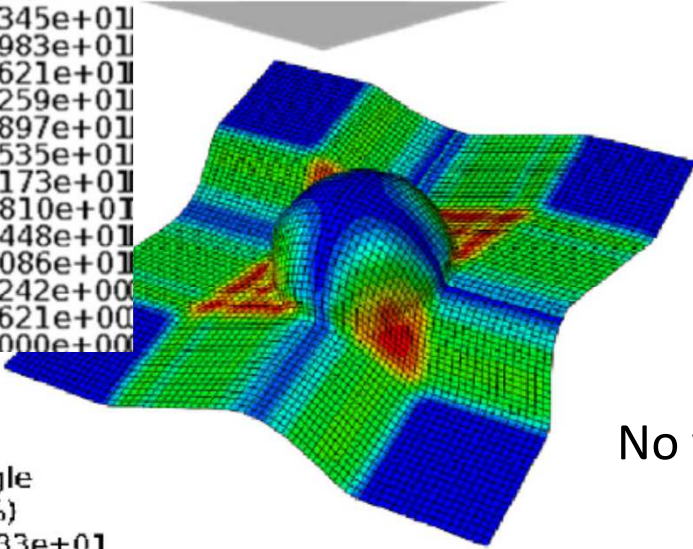
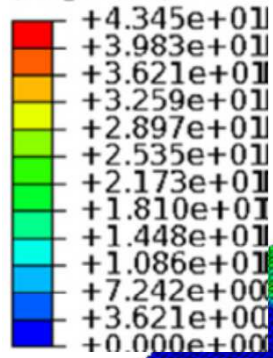


FE models for the forming simulations

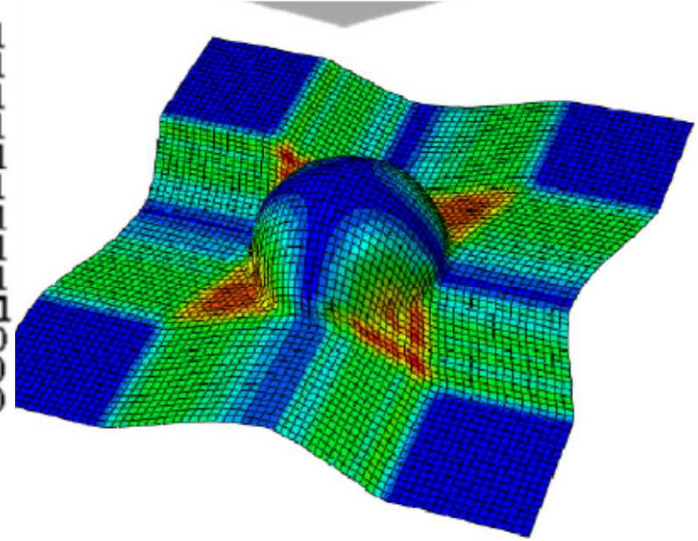
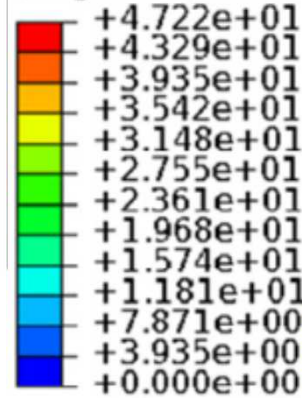


# Macroscopic forming simulations

Shear angle  
(Avg: 75%)

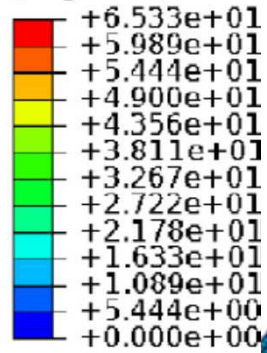


Shear angle  
(Avg: 75%)

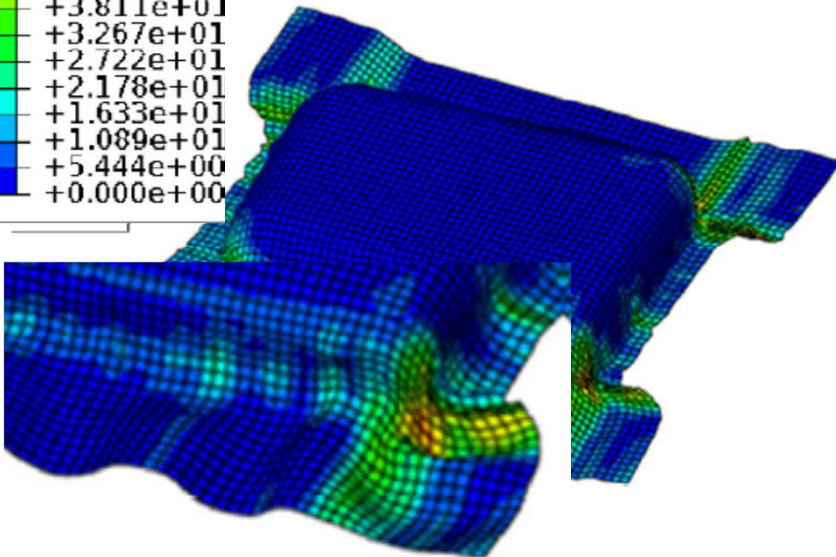


No wrinkles

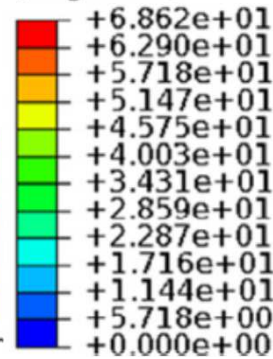
Shear angle  
(Avg: 75%)



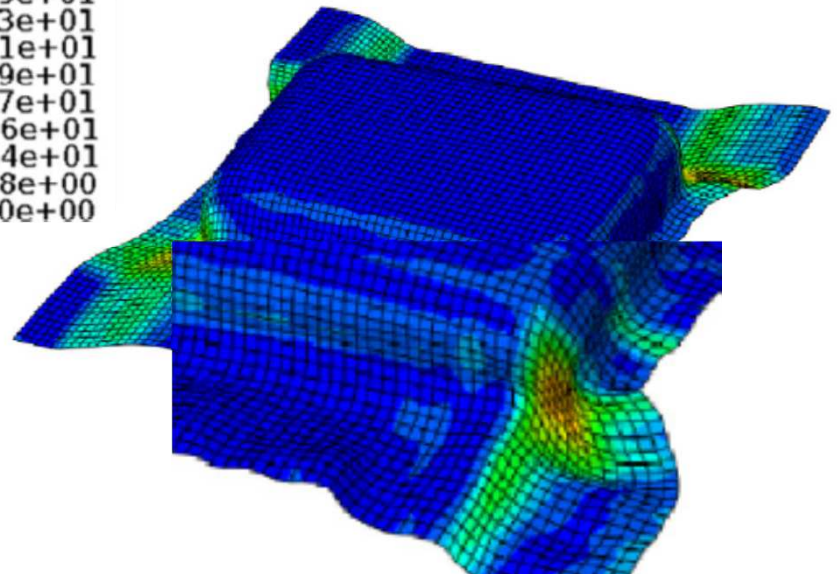
Fabric A



Shear angle  
(Avg: 75%)

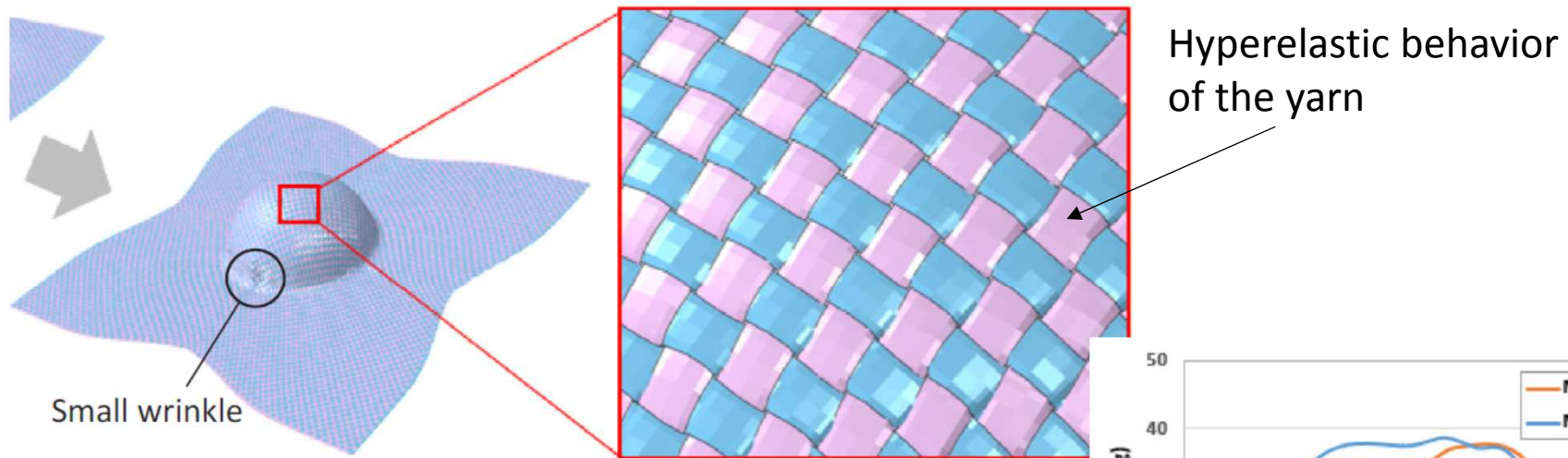


Fabric B

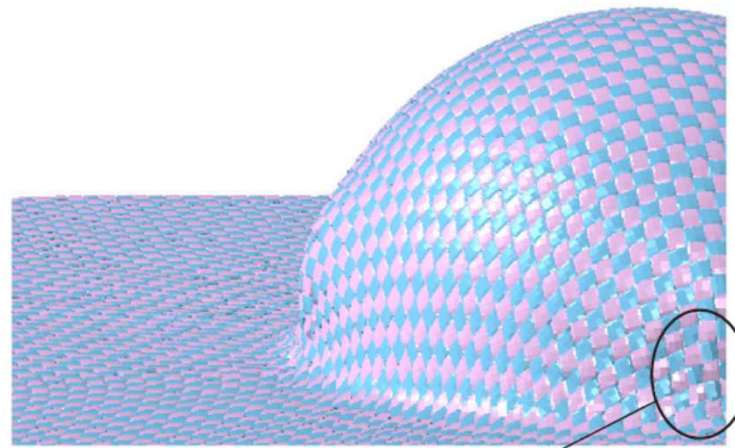
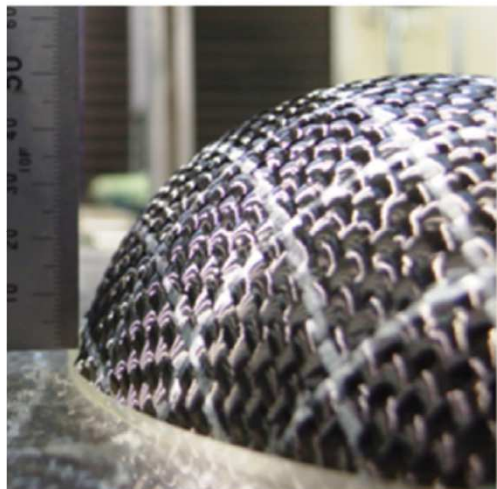
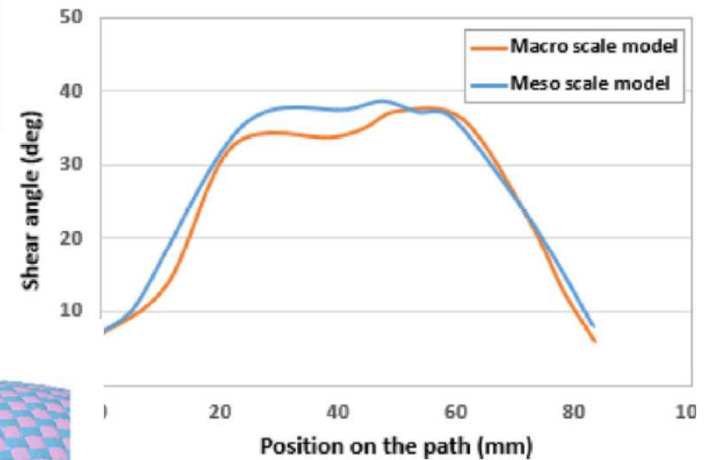


e

# Large scale meso model (Fabric A)



small wrinkles appear, which are not predicted in the macro-scale simulation



Small wrinkle

**10 days of calculation**

four CPUs  
(Xeon E5-2690v4: 2.6 GHz)  
and  
memory size of 16 GB

Calculation cost, hemispherical mould.

Type of simulation	Total CPU time	
	Fabric A	Fabric B
Macro scale	36 min	31 min
Large meso scale	258 h	No convergence
MMZ	44 h	15 h

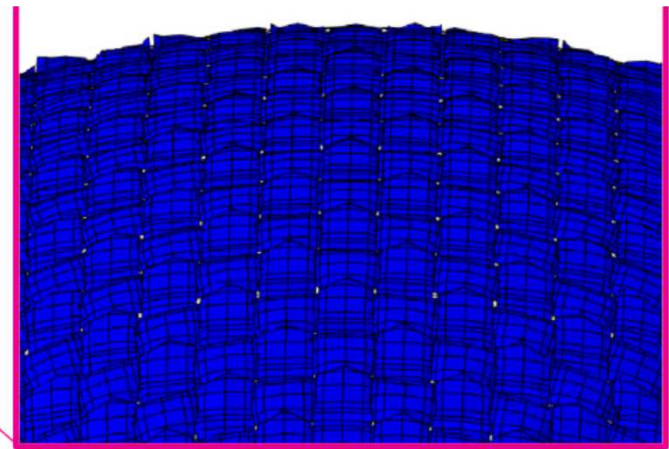
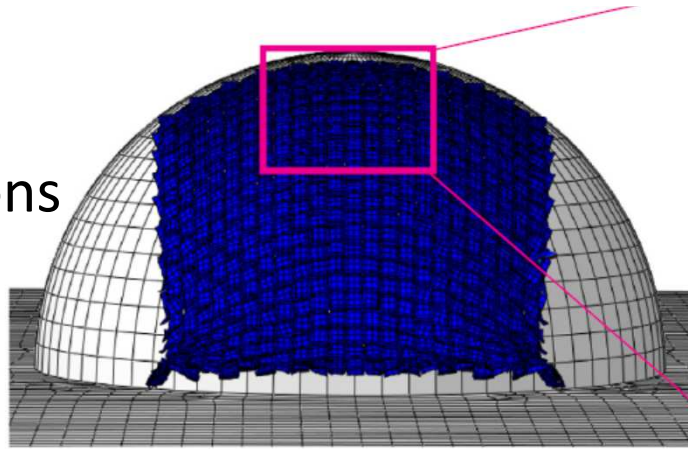
### Macro-meso zoom simulation of draping (MZZ)

The meso-calculations use **the boundary conditions obtained from the macro-calculations**. The displacements along the edge of the meso-“patch”, were extracted from the macro-calculation results along the path corresponding to the edge. The yarns in the meso-calculation are also under contact conditions with the mould and the acrylic plate.



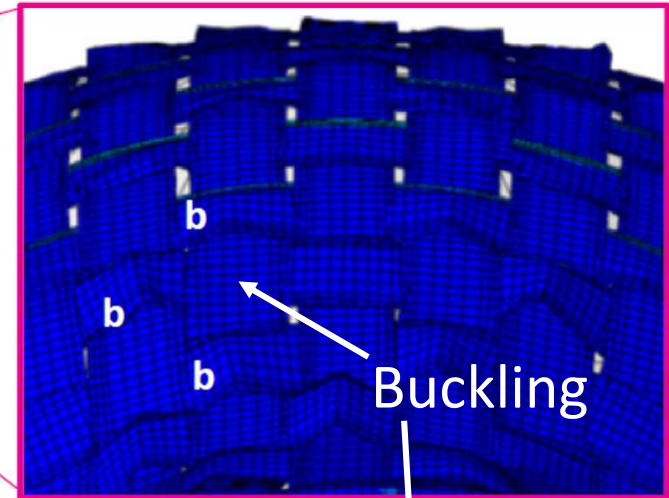
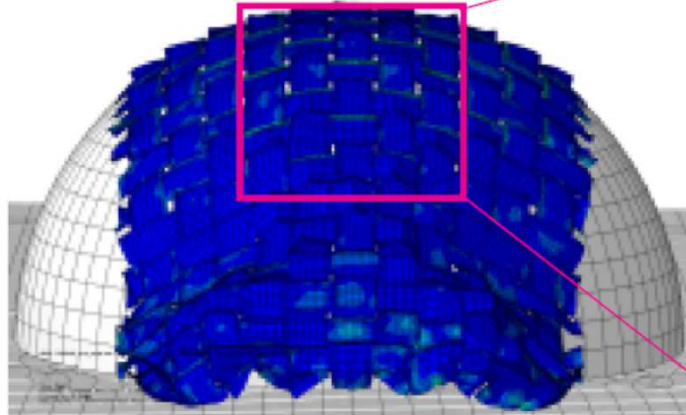
# MMZ simulations

Fabric A  
No buckling

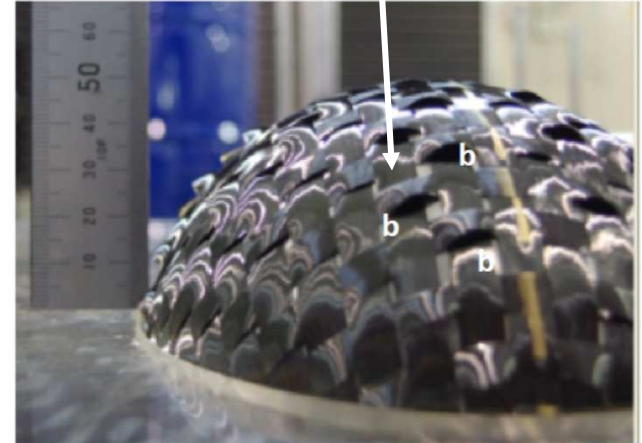
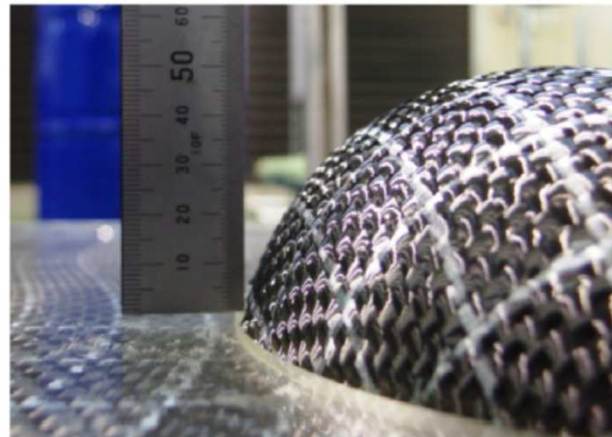


d

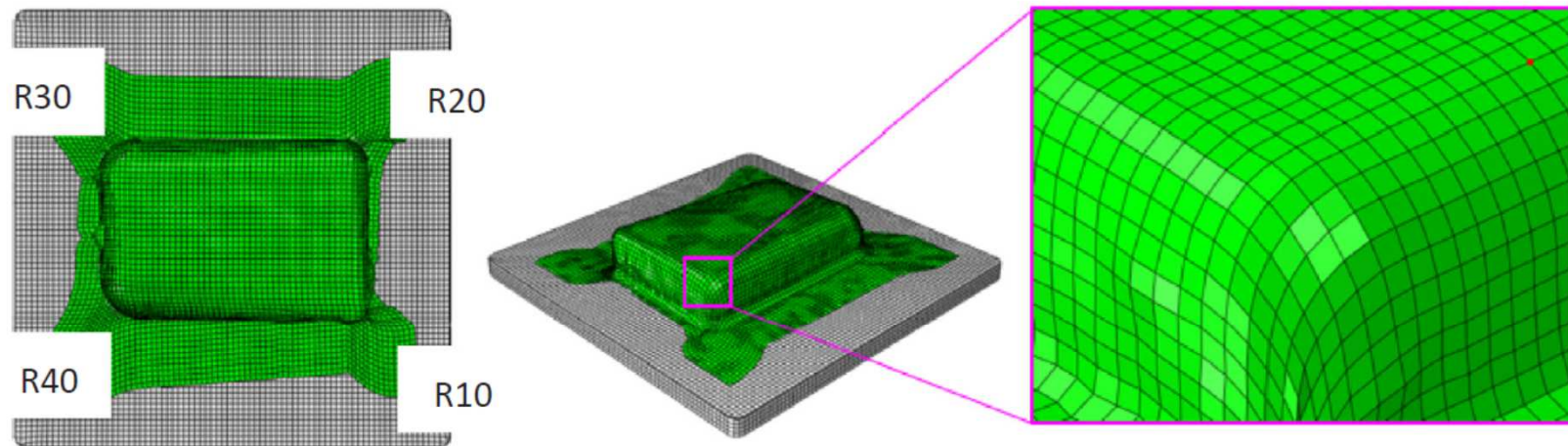
Fabric B  
Some bucklings



The buckling happens in the low-shear-angle zone of the draped fabric.

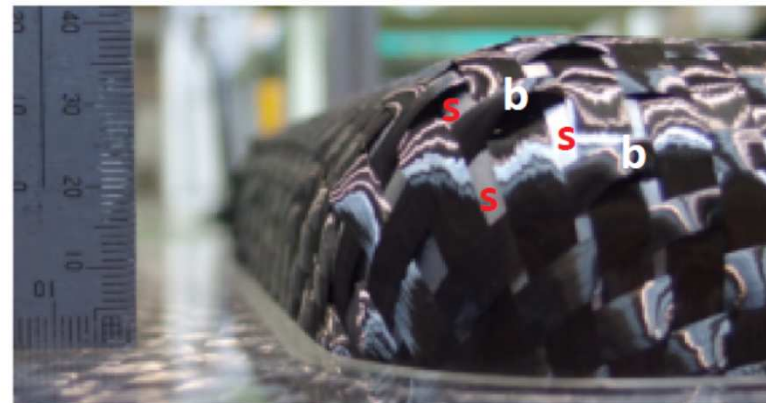
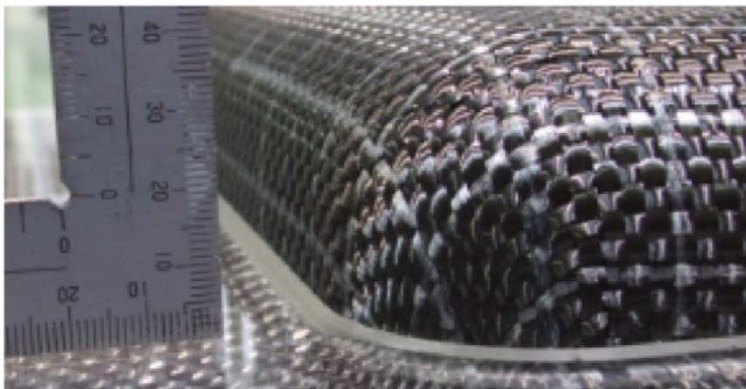


# MMZ simulation : Box shape mould



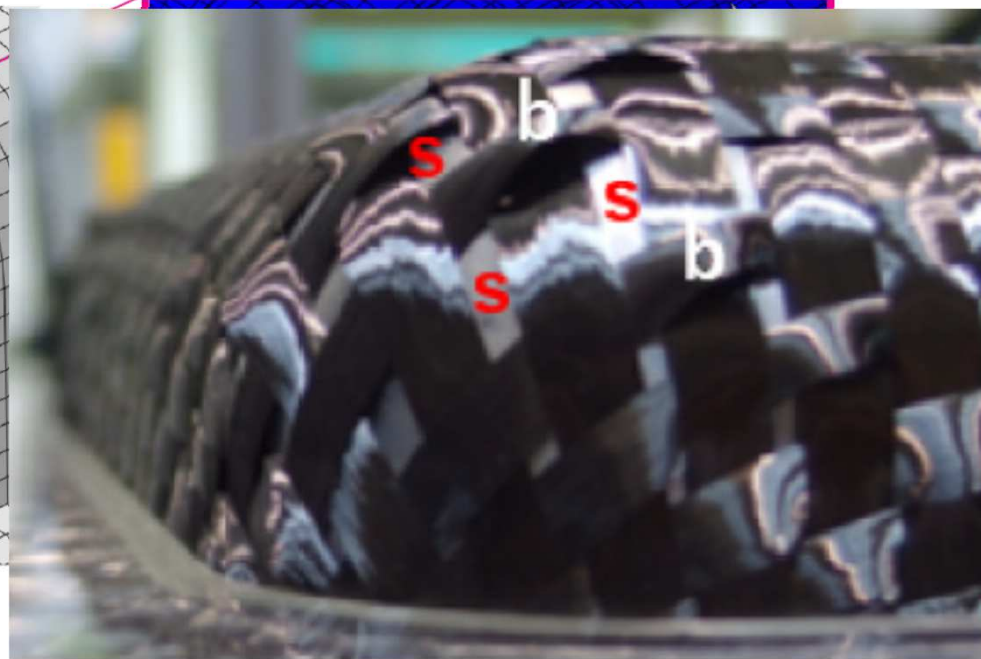
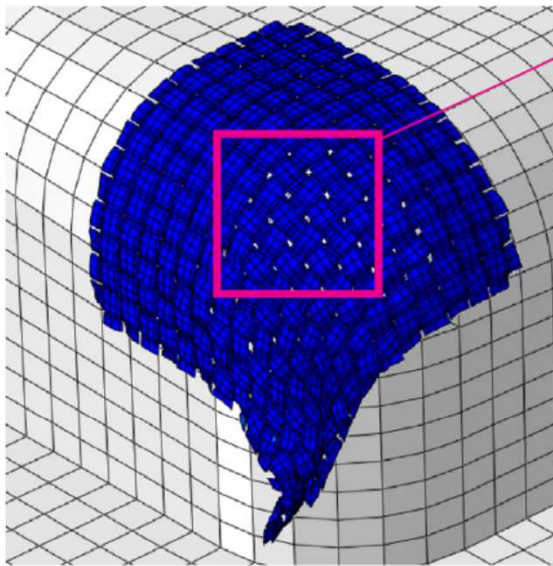
the meso-zoom region

a

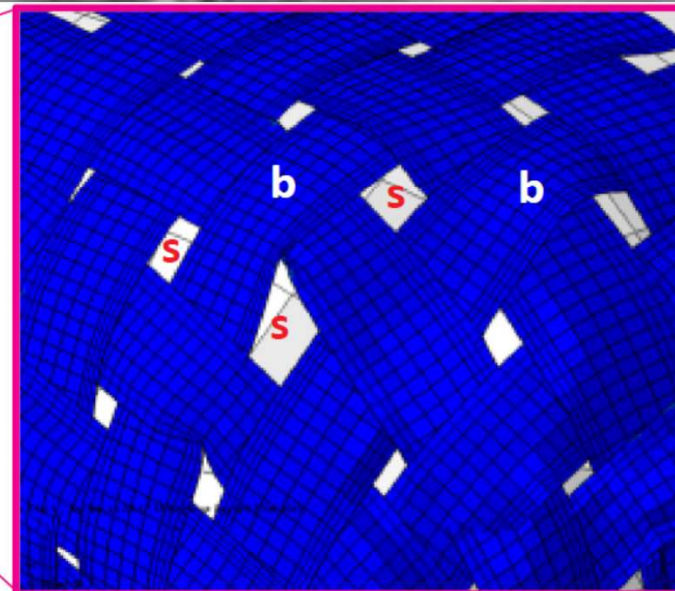
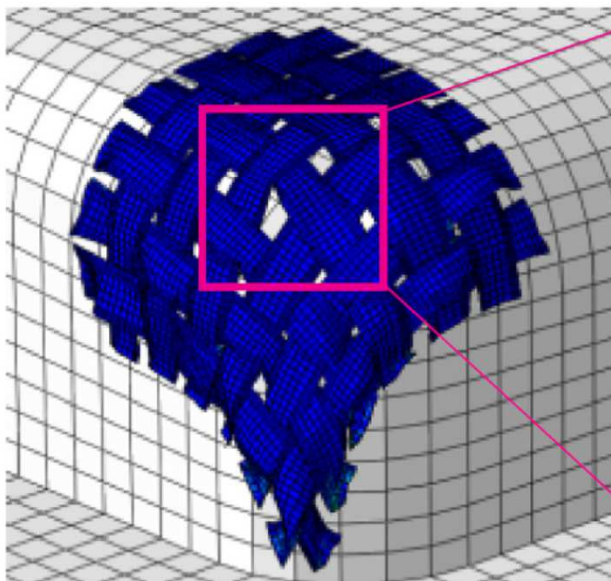




Fabric A



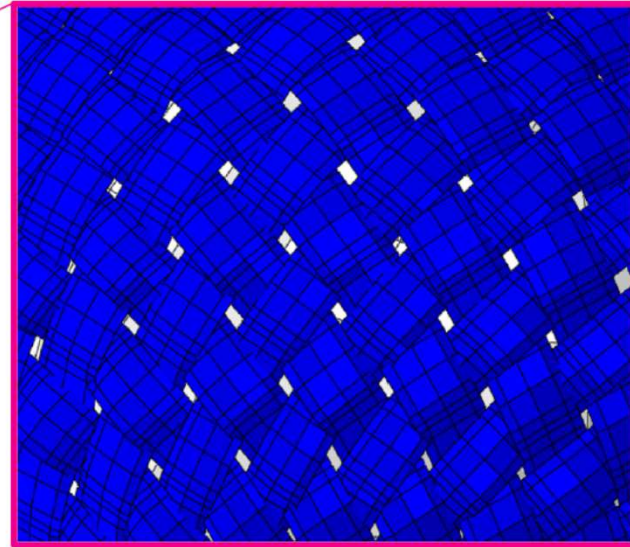
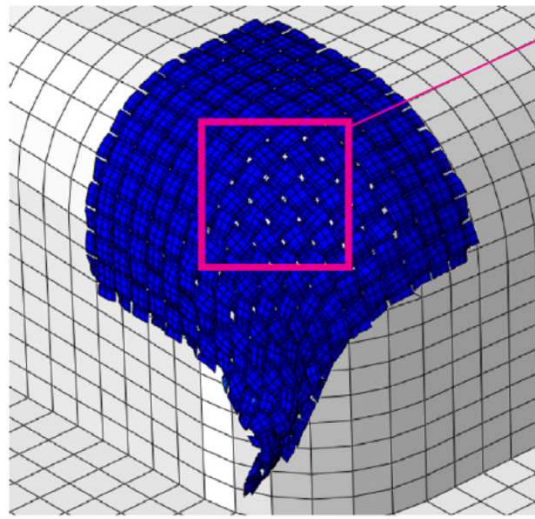
Fabric B



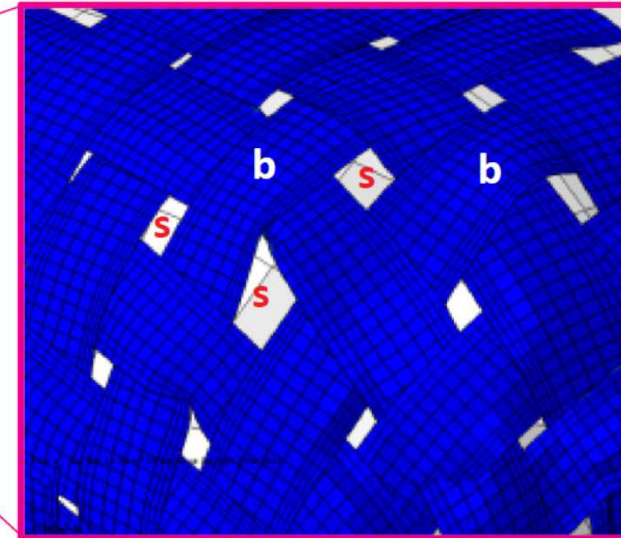
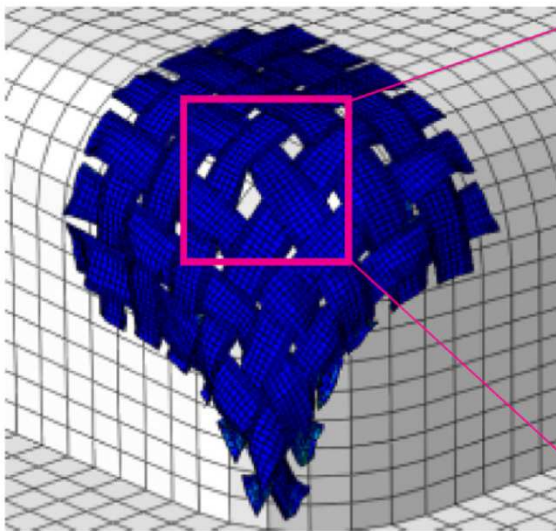
b – buckling S-sliding<sup>20</sup>



Fabric A



Fabric B



More details in [Iwata et al, Composites A, 2019]

A 3D rendered yellow mesh grid on a blue background. The grid consists of thick, yellow, textured bands that intersect to form a series of rectangular openings. The bands have a fine, grid-like texture and are set against a solid blue background.

**Thank you for your attention**